

# *asprin*: Answer Set Programming with Preferences

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# Outline

- 1 Introduction
- 2 Declarative Problem Solving
- 3 An Example
- 4 Preliminaries
- 5 Language
- 6 Implementation
- 7 Experimental analysis
  - Boosting optimization via heuristics
  - Dedicated systems versus asprin
- 8 Summary

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# Motivation

- Answer Set Programming (ASP) is an approach to declarative problem solving, combining
  - a rich yet simple modeling language
  - with high-performance solving capacities
- tailored to Knowledge Representation and Reasoning
- ASP allows for solving all search problems in  $NP$  (and  $NP^{NP}$ ) in a uniform way
- ASP is versatile as reflected by the ASP solver *clingo*, winning first places at ASP, CASC, MISC, PB, and SAT competitions
- ASP embraces many emerging application areas, and users

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- For real-world applications, the identification of preferred, or optimal, solutions is often indispensable
  - In many cases, this also involves the combination of various qualitative and quantitative preferences
- Only optimization statements representing objective functions using summation are established components of today's ASP systems
- Example `#minimize{40 : coast; 70 : mountain}`

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- Example `#minimize{40 : coast; 70 : mountain}`

# Approach

- **asprin** is a framework for handling preferences among the (stable) models of logic programs
  - general because it captures many existing approaches to preference
  - flexible because it allows combining different types of preferences
  - extensible, allowing for an easy implementation of new approaches to preferences

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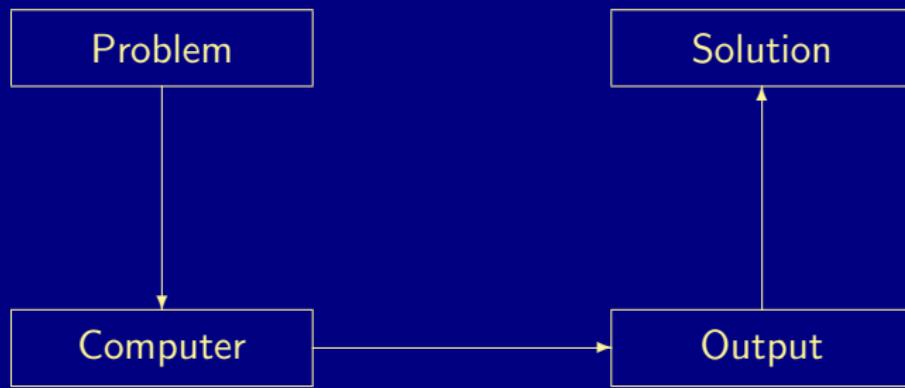
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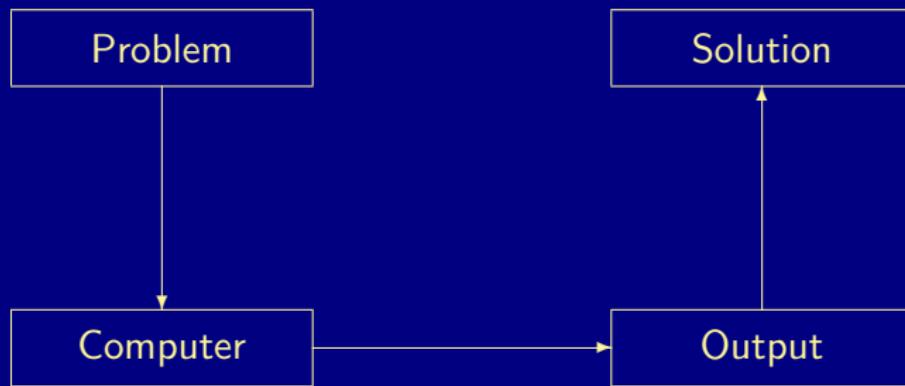
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*"What is the problem?"* versus *"How to solve the problem?"*



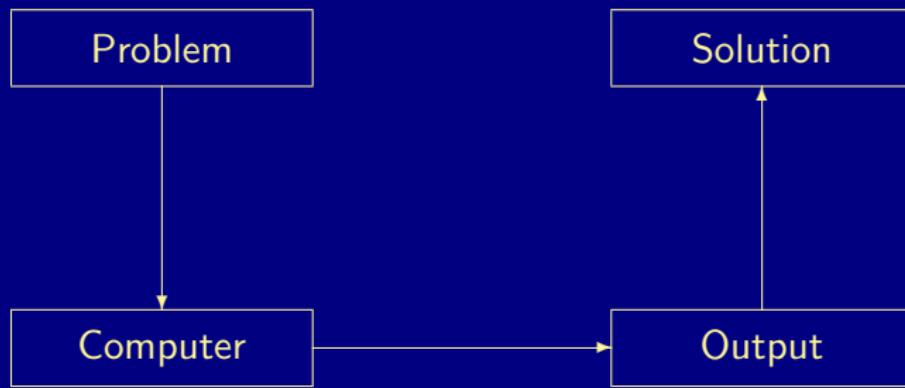
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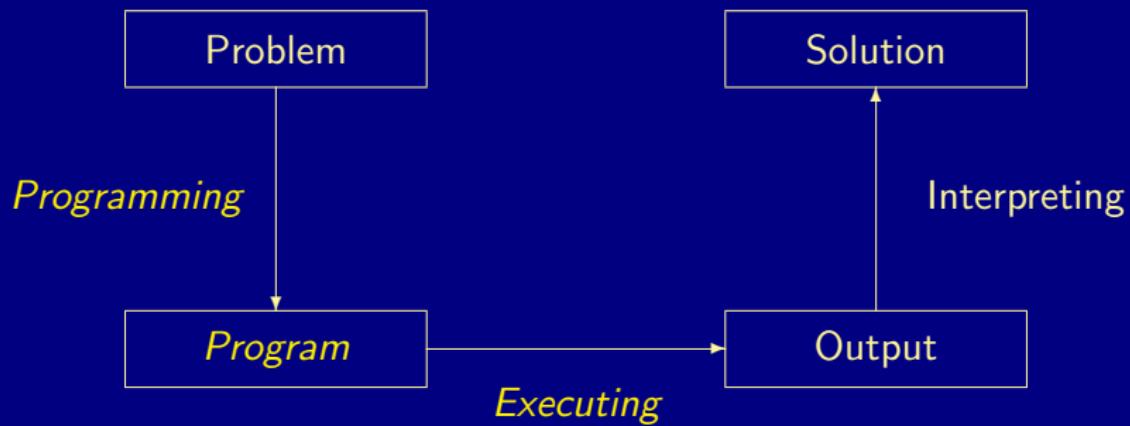
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*"What is the problem?"* versus *"How to solve the problem?"*



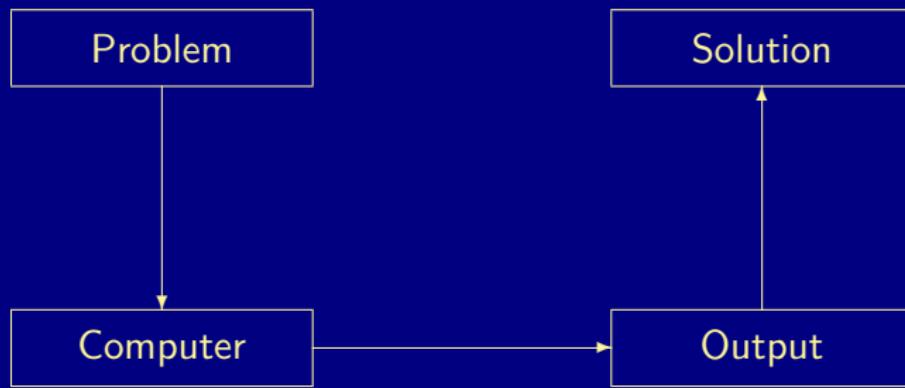
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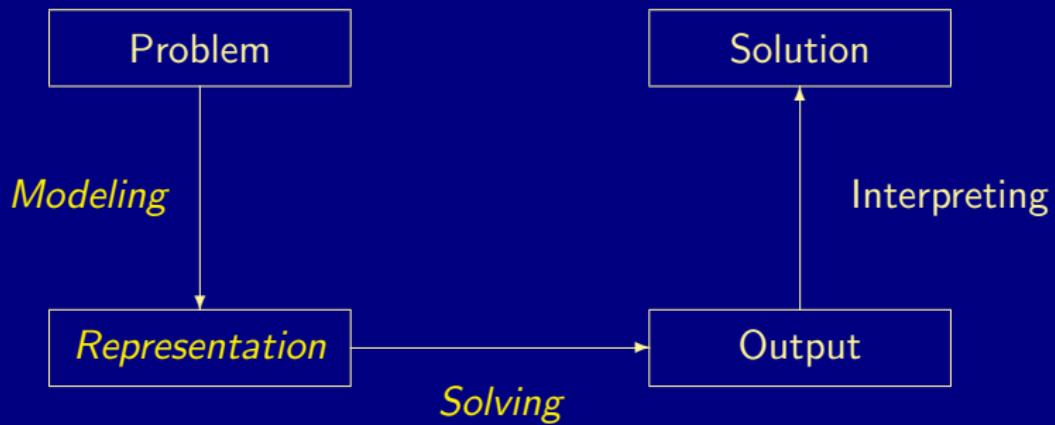
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*"What is the problem?"*    versus    *"How to solve the problem?"*



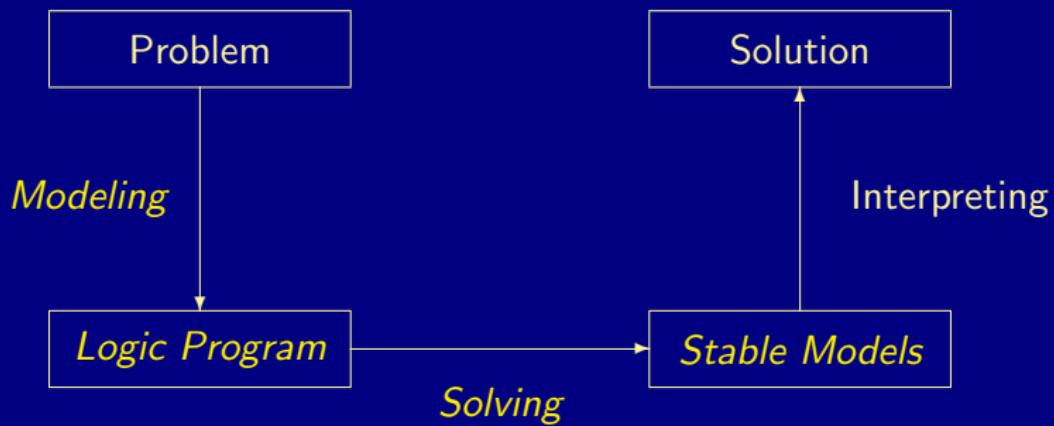
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# ASP for Declarative problem solving

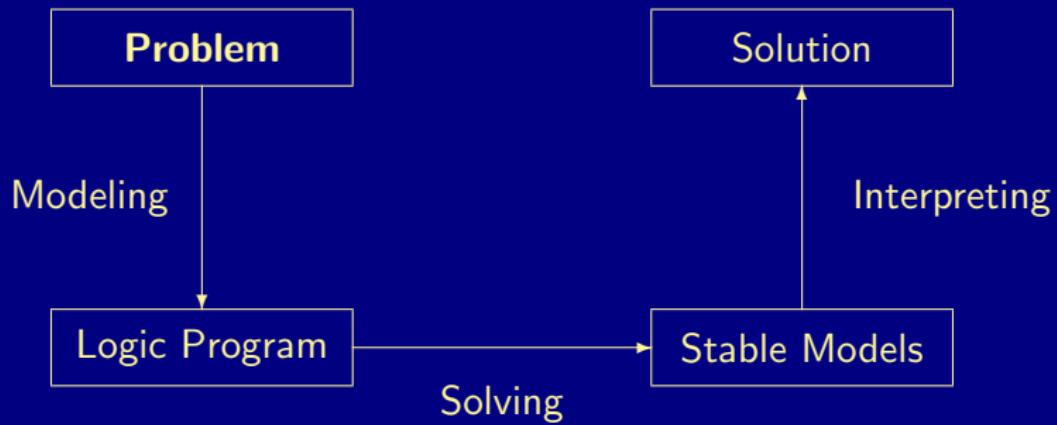
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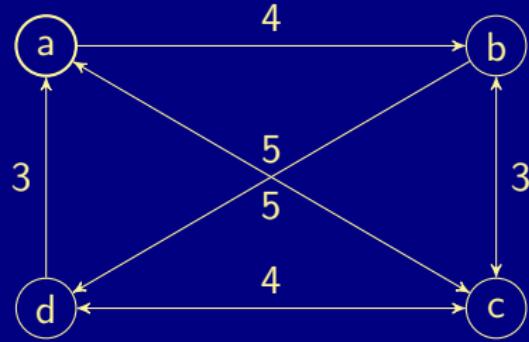
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# An Example: Travelling Salesperson



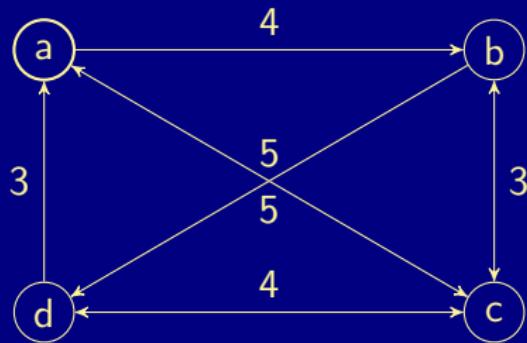
# Travelling Salesperson

- Problem instance A map with cities, directed roads with distances, and one starting city
- Problem class Find a route visiting every city once, and returning to the starting city

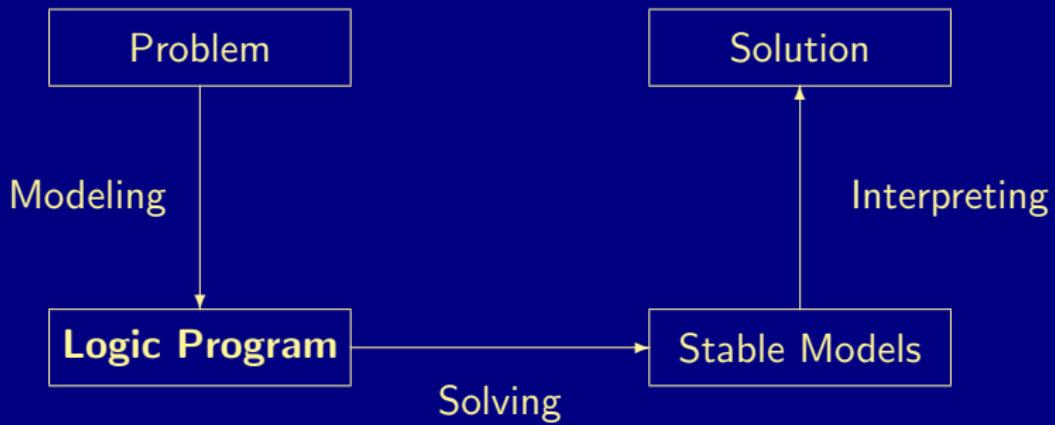


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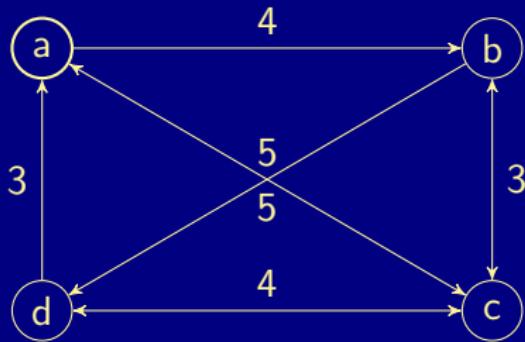


# Travelling Salesperson



# Travelling Salesperson

- Problem instance A map with cities, directed roads with distances, and one starting city



```
city(a). city(b). city(c). city(d). start(a).
road(a,b,4). road(a,c,5). road(b,c,3). road(b,d,5).
road(c,a,5). road(c,b,3). road(c,d,4).
road(d,a,3). road(d,c,4).
```

# Travelling Salesperson

- Problem class Find a route visiting every city once, and returning to the starting city

```
{ travel(X,Y) } :- road(X,Y,D).
```

```
visited(Y) :- start(X), travel(X,Y).
```

```
visited(Y) :- visited(X), travel(X,Y).
```

```
:- city(X), not visited(X).
```

```
:- city(X), 2 { travel(X,Y) }.
```

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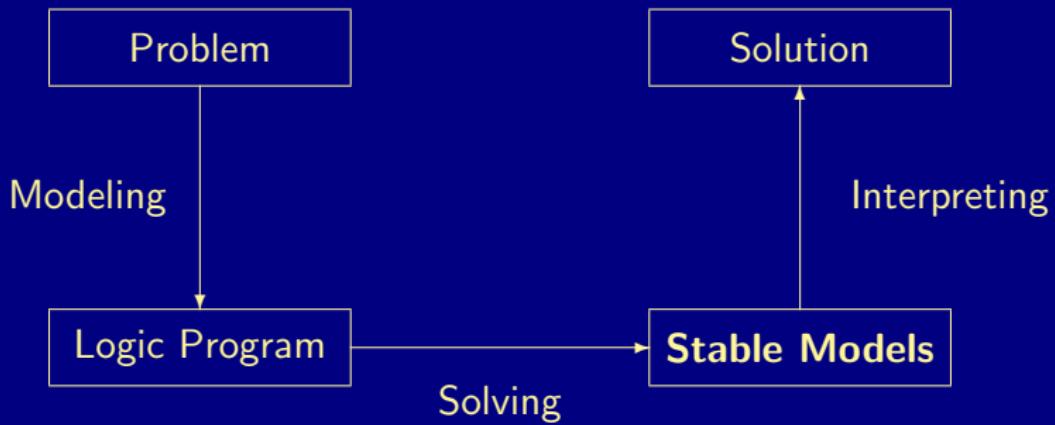
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```

# Travelling Salesperson



# Travelling Salesperson

```
$ clingo tsp.lp 0
```

```
clingo version 5.1.0
```

```
Reading from tsp.lp
```

```
Solving...
```

```
Answer: 1
```

```
travel(a,b) travel(b,c) travel(c,d) travel(d,a) ...
```

```
Answer: 2
```

```
travel(a,b) travel(b,d) travel(d,c) travel(c,a) ...
```

```
Answer: 3
```

```
travel(a,c) travel(c,b) travel(b,d) travel(d,a) ...
```

```
SATISFIABLE
```

```
Models : 3
```

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Reading from tsp.lp
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Solving...
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Answer: 1
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travel(a,b) travel(b,c) travel(c,d) travel(d,a) ...
```

```
Answer: 2
```

```
travel(a,b) travel(b,d) travel(d,c) travel(c,a) ...
```

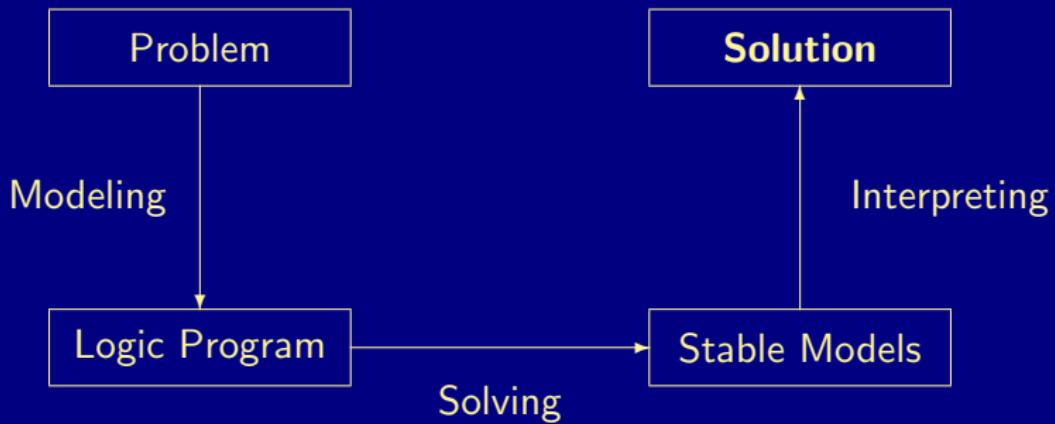
```
Answer: 3
```

```
travel(a,c) travel(c,b) travel(b,d) travel(d,a) ...
```

```
SATISFIABLE
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```
Models : 3
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# Travelling Salesperson



# A route

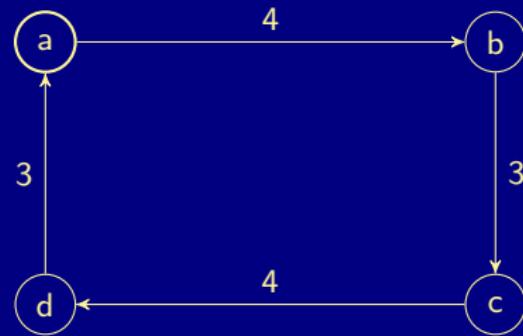
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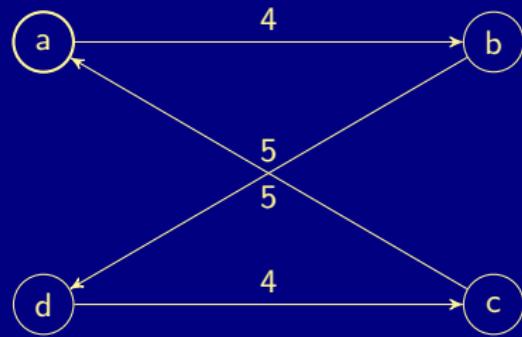
travel(a,b) travel(b,c) travel(c,d) travel(d,a) ...



## A route

Answer: 2

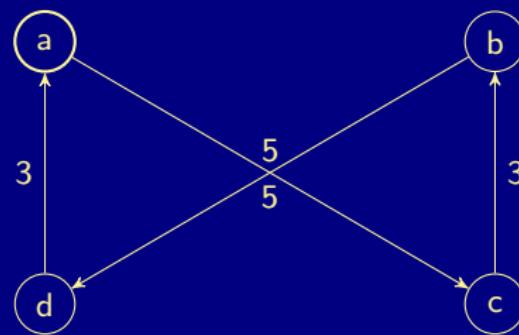
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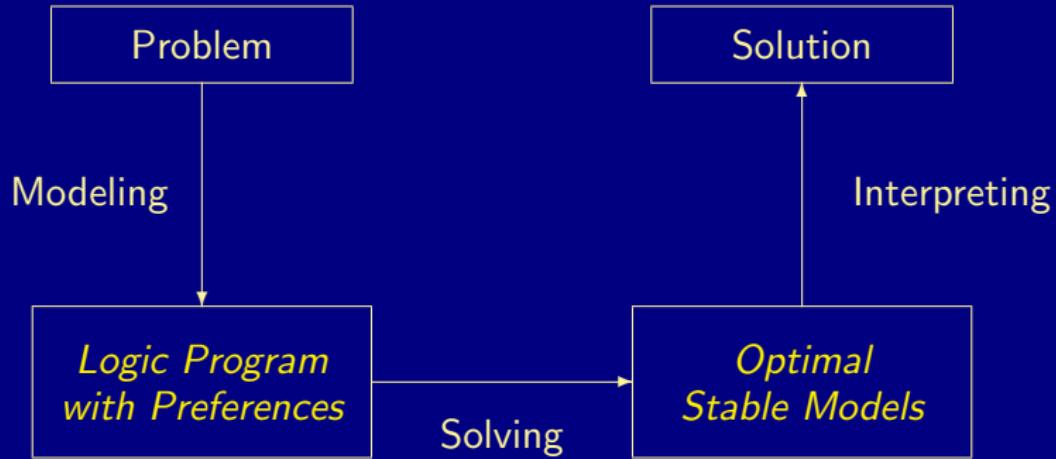
## A route

Answer: 3

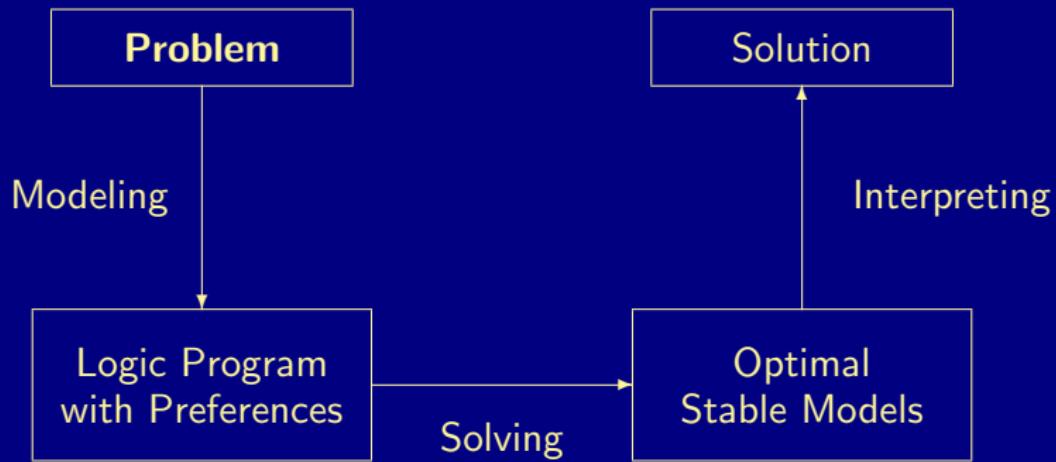
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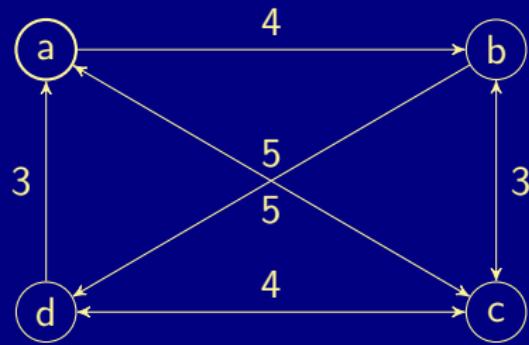


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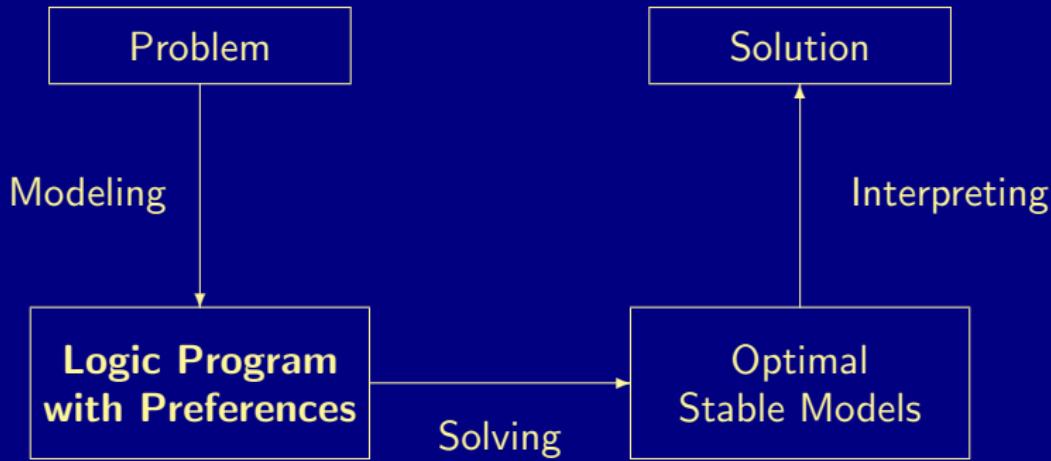


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- Problem class Find a route visiting every city once, and returning to the starting city. *Prefer routes of minimum distance.*



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#preference(distance,less(weight)){  
    D,(X,Y) :: travel(X,Y), road(X,Y,D)  
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#optimize(distance).
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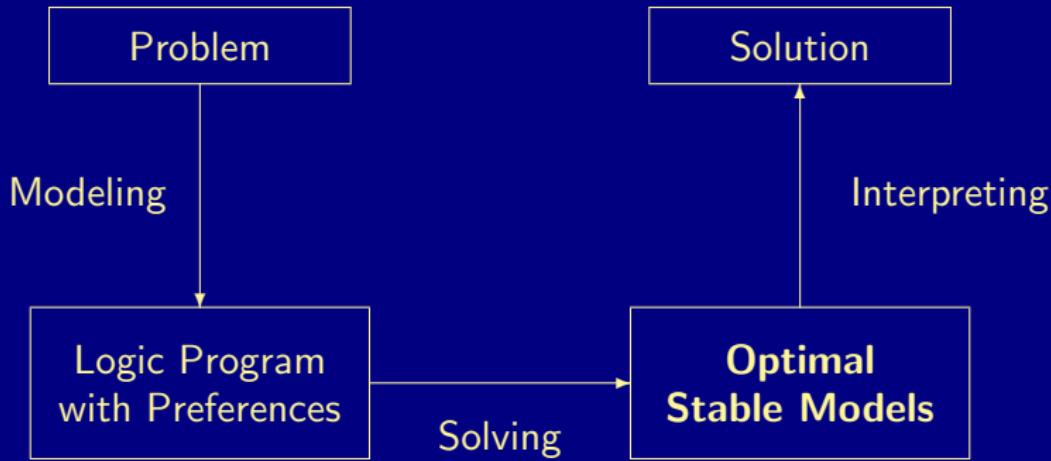
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# Travelling Salesperson



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```
$ asprin tsp.lp preference.lp 0
```

```
asprin version 3.0.0
```

```
Reading from tsp.lp ...
```

```
Solving...
```

```
Answer: 1
```

```
travel(a,c) travel(c,b) travel(b,d) travel(d,a) ...
```

```
Answer: 2
```

```
travel(a,b) travel(b,c) travel(c,d) travel(d,a) ...
```

```
OPTIMUM FOUND
```

```
Models : 2
```

```
Optimum : yes
```

```
Optimal : 1
```

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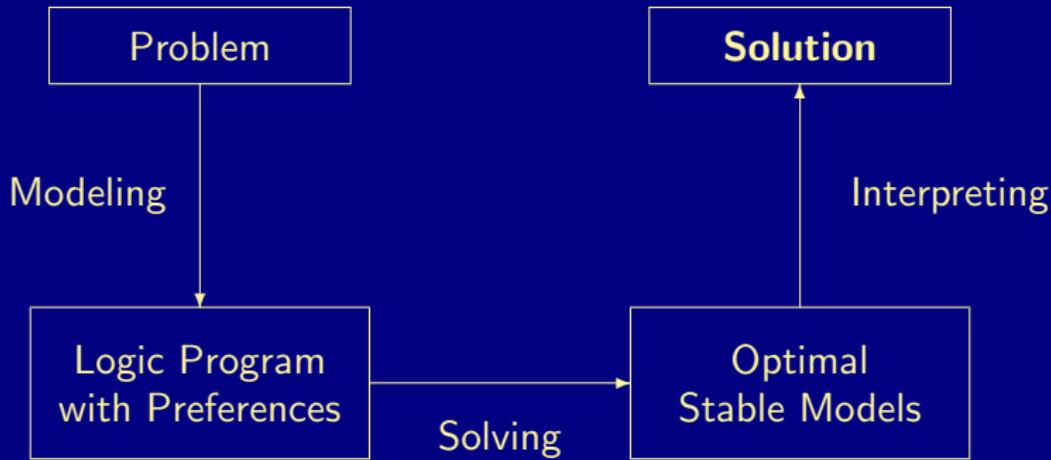
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Models : 2
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# Travelling Salesperson



## A route

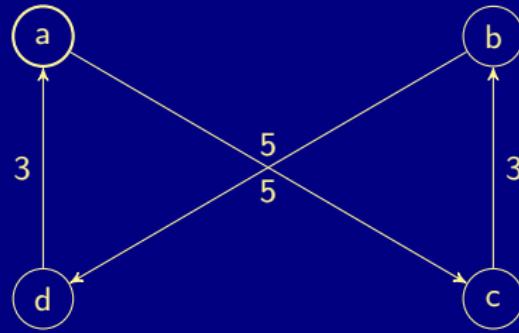
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OPTIMUM FOUND



# An optimal route

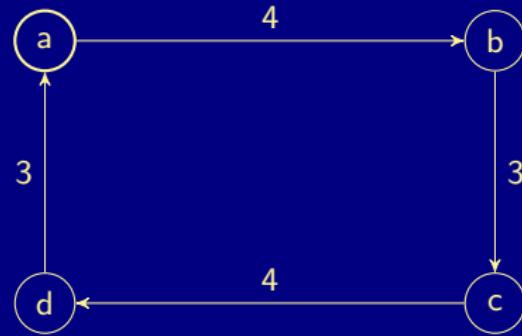
Answer: 1

travel(a,c) travel(c,b) travel(b,d) travel(d,a) ...

Answer: 2

travel(a,b) travel(b,c) travel(c,d) travel(d,a) ...

OPTIMUM FOUND



# Extending Travelling Salesperson

- Problem class Find a route visiting every city once, and returning to the starting city. *Prefer going along the outside coast if it is cloudy, else prefer going through the inside mountains.*

```
type(X,Y,mountain) :- road(X,Y,D), D == 5.
type(X,Y,coast)    :- road(X,Y,D), D != 5.

#preference(weather,aso){
    travel(X,Y), type(X,Y,coast) >>
        travel(X',Y), type(X',Y,mountain) || cloudy;
    travel(X,Y), type(X,Y,mountain) >>
        travel(X',Y), type(X',Y,coast) || not cloudy
}.
#optimize(weather).
```

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# Extending Travelling Salesperson

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```

```
asprin version 3.0.0
```

```
Reading from tsp.lp ...
```

```
Solving...
```

```
Solving...
```

```
Answer: 1
```

```
travel(a,b) travel(b,c) travel(c,d) travel(d,a)
```

```
Answer: 2
```

```
travel(a,c) travel(b,d) travel(c,b) travel(d,a)
```

```
OPTIMUM FOUND
```

```
Answer: 3
```

```
travel(a,b) travel(b,d) travel(c,a) travel(d,c)
```

```
OPTIMUM FOUND
```

Models : 3

Optimum : yes

Optimal : 2

# Extending Travelling Salesperson

```
$ asprin tsp.lp preference.lp 0

asprin version 3.0.0
Reading from tsp.lp ...
Solving...
Solving...
Answer: 1
travel(a,b) travel(b,c) travel(c,d) travel(d,a)
Answer: 2
travel(a,c) travel(b,d) travel(c,b) travel(d,a)
OPTIMUM FOUND
Answer: 3
travel(a,b) travel(b,d) travel(c,a) travel(d,c)
OPTIMUM FOUND

Models : 3
Optimum : yes
Optimal : 2
```

# Extending Travelling Salesperson

- Problem class Find a route visiting every city once, and returning to the starting city. Prefer routes of minimum distance. Prefer going through the outside coast if it is cloudy, else prefer going through the inside mountains. *Combine both preferences with Pareto.*

```
#preference(all,pareto){  
    **distance;  
    **weather  
}.  
#optimize(all).
```

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- Problem class Find a route visiting every city once, and returning to the starting city. Prefer routes of minimum distance. Prefer going through the outside coast if it is cloudy, else prefer going through the inside mountains. *Combine both preferences with Pareto.*

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```

```
Solving...
```

```
Answer: 1
```

```
travel(a,b) travel(b,c) travel(c,d) travel(d,a)
```

```
OPTIMUM FOUND
```

```
Answer: 2
```

```
travel(a,c) travel(b,d) travel(c,b) travel(d,a)
```

```
OPTIMUM FOUND
```

```
Answer: 3
```

```
travel(a,b) travel(b,d) travel(c,a) travel(d,c)
```

```
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Models : 3
```

```
Optimum : yes
```

```
Optimal : 3
```

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Reading from tsp.lp ...
Solving...
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travel(a,b) travel(b,c) travel(c,d) travel(d,a)
OPTIMUM FOUND
Answer: 2
travel(a,c) travel(b,d) travel(c,b) travel(d,a)
OPTIMUM FOUND
Answer: 3
travel(a,b) travel(b,d) travel(c,a) travel(d,c)
OPTIMUM FOUND

Models : 3
Optimum : yes
Optimal : 3
```

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# Preference

- A strict partial order  $\succ$  on the stable models of a logic program  
That is,  $X \succ Y$  means that  $X$  is preferred to  $Y$
- A stable model  $X$  is  $\succ$ -preferred, if there is no other stable model  $Y$  such that  $Y \succ X$
- A preference type is a (parametric) class of preference relations
- Example *subset*, *pareto*, etc.

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- A preference type is a (parametric) class of preference relations
- Example *subset*, *pareto*, etc.

# Preference

- A strict partial order  $\succ$  on the stable models of a logic program  
That is,  $X \succ Y$  means that  $X$  is preferred to  $Y$
- A stable model  $X$  is  $\succ$ -preferred, if there is no other stable model  $Y$  such that  $Y \succ X$
- A preference type is a (parametric) class of preference relations
- Example *subset*, *pareto*, etc.

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- 1 Introduction
- 2 Declarative Problem Solving
- 3 An Example
- 4 Preliminaries
- 5 Language
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- 7 Experimental analysis
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# Language

- naming atom

**\*\*s**

where  $s$  is the name of a preference

- weighted formula

$w_1, \dots, w_l : \phi$

where each  $w_i$  is a term and  $\phi$  is a Boolean formula

- preference element

$\Phi_1 \gg \dots \gg \Phi_m \parallel \Phi_{m+1}$

where each  $\Phi_r$  is a set of weighted formulas

- preference statement

$\#preference(s, t)\{e_1, \dots, e_n\}$

where  $s$  and  $t$  represent the preference statement and its type  
and each  $e_j$  is a preference element

- optimization directive

$\#optimize(s)$

where  $s$  is the name of a preference

- preference specification is a set  $S$  of preference statements and a directive

$\#optimize(s)$  such that  $S$  is acyclic, closed, and  $s \in S$

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# Preference type

- A preference type  $t$  is a function mapping a set of preference elements  $E$  to a preference relation

$$t(E) \subseteq \mathcal{A} \times \mathcal{A}$$

- Examples

$$(X, Y) \in \text{subset}(E) \text{ iff } \{\ell \in E \mid X \models \ell\} \subset \{\ell \in E \mid Y \models \ell\}$$

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- Reification  $H_X = \{ \text{holds}(a) \mid a \in X\}$  and  $H'_X = \{ \text{holds}'(a) \mid a \in X\}$
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We define  $Q_s$  as a preference program for  $s$ , if for all sets  $X, Y \subseteq \mathcal{A}$ , we have

$X \succ_s Y$  iff  $Q_s \cup H_X \cup H'_Y$  is satisfiable

- Note  $Q_s$  is implemented as  $F_s \cup E_{t_s} \cup C$
- Note *asprin's* expressiveness is delineated by the decision problem

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$$\#\text{preference}(1, \text{subset})\{a, b, c\}$$

$$\#\text{optimize}(1)$$

$$H_{\{a\}} = \left\{ \text{holds}(a). \right\}$$

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$$F_1 = \left\{ \begin{array}{ll} \text{preference}(1, \text{subset}). & \text{preference}(1, 1, 1, \text{for}(a), ()). \\ \text{optimize}(1). & \text{preference}(1, 2, 1, \text{for}(b), ()). \\ & \text{preference}(1, 3, 1, \text{for}(c), ()). \end{array} \right\}$$

$$E_{\text{subset}} = \left\{ \begin{array}{l} \text{better}(P) : - \text{preference}(P, \text{subset}), \\ \quad \text{not holds}(X), \quad \text{holds}'(X), \quad \text{preference}(P, \_, \_, \text{for}(X), \_), \\ \quad \text{not holds}(Y) : \text{not holds}'(Y), \quad \text{preference}(P, \_, \_, \text{for}(Y), \_). \end{array} \right\}$$

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There is no stable model, indicating that  $\{a, b\} \not\succ_1 \{a\}$

## Basic algorithm $solveOpt(P, s)$

**Input** : A program  $P$  over  $\mathcal{A}$  and preference statement  $s$

**Output** : A  $\succ_s$ -preferred stable model of  $P$ , if  $P$  is satisfiable, and  $\perp$  otherwise

```
 $Y \leftarrow solve(P)$ 
if  $Y = \perp$  then return  $\perp$ 
repeat
|    $X \leftarrow Y$ 
|    $Y \leftarrow solve(P \cup Q_s \cup R \cup H'_X)$ 
until  $Y = \perp$ 
return  $X$ 
```

where  $R = \{holds(a) \leftarrow a \mid a \in \mathcal{A}\}$

*asprin's library*

## ■ Basic preference types

- subset and superset
- less(cardinality) and more(cardinality)
- less(weight) and more(weight)
- maxmin and minmax
- aso (Answer Set Optimization)
- poset (Qualitative Preferences)

## ■ Composite preference types

- neg
- and
- pareto
- lexico

## ■ And more to come...

- cp (restricted CP nets)

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# Heuristic framework

- *clingo* allows for incorporating domain-specific heuristics into ASP solving
  - input language for expressing domain-specific heuristics
  - solving capacities for integrating domain-specific heuristics
- Heuristic directive `#heuristic`
- Heuristic modifiers (atom,  $a$ , and integer,  $v$ )
  - init for initializing the heuristic value of  $a$  with  $v$
  - factor for amplifying the heuristic value of  $a$  by factor  $v$
  - level for ranking all atoms; the rank of  $a$  is  $v$
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#heuristic occurs(mv,5) : action(mv), time(5). [5,factor]
```

# *asprin* with different heuristic settings

| Benchmark \ System             |      | <i>asprin<sub>w</sub></i> | <i>asprin<sub>w+s</sub></i> | <i>asprin<sub>w+1</sub></i> | <i>asprin<sub>w+f</sub></i> | <i>asprin<sub>s</sub></i> | <i>asprin<sub>s+s</sub></i> | <i>asprin<sub>s+1</sub></i> | <i>asprin<sub>s+f</sub></i> |             |
|--------------------------------|------|---------------------------|-----------------------------|-----------------------------|-----------------------------|---------------------------|-----------------------------|-----------------------------|-----------------------------|-------------|
| <i>Ricochet</i>                | (30) | 20.00                     | 432 ( 8, 4)                 | 407 ( 7, 4)                 | 68 ( 1, 0)                  | 71 (1, 0)                 | 365 ( 8, 3)                 | 461 ( 7, 10)                | 69 (1, 0)                   | 71 (1, 0)   |
| <i>Timetabling</i>             | (12) | 23687.75                  | 345 (285, 3)                | 255 (202, 2)                | 900 ( 4, 12)                | 6 (1, 0)                  | 217 (144, 2)                | 21 (18, 0)                  | 900 (2, 12)                 | 5 (1, 0)    |
| <i>Puzzle</i>                  | (7)  | 580.57                    | 82 ( 2, 0)                  | 112 ( 2, 0)                 | 136 ( 2, 0)                 | 416 (2, 1)                | 31 ( 1, 0)                  | 32 ( 1, 0)                  | 21 (1, 0)                   | 51 (1, 0)   |
| <i>Crossing</i>                | (24) | 211.92                    | 104 ( 42, 1)                | 98 ( 35, 0)                 | 805 (19, 20)                | 387 (6, 6)                | 0 ( 6, 0)                   | 1 ( 6, 0)                   | 7 (9, 0)                    | 3 (1, 0)    |
| <i>Valves</i>                  | (30) | 56.63                     | 69 ( 7, 0)                  | 65 ( 6, 0)                  | 460 ( 8, 11)                | 715 (0, 22)               | 38 ( 4, 0)                  | 39 ( 4, 0)                  | 339 (4, 6)                  | 673 (0, 21) |
| <i>Expansion</i>               | (30) | 7501.87                   | 216 (299, 0)                | 10 ( 15, 0)                 | 38 ( 7, 0)                  | 12 (3, 0)                 | 64 (295, 0)                 | 14 (54, 0)                  | 4 (4, 0)                    | 3 (1, 0)    |
| <i>Repair</i>                  | (30) | 6750.73                   | 76 ( 48, 0)                 | 15 ( 47, 0)                 | 71 ( 3, 2)                  | 8 (2, 0)                  | 8 ( 43, 0)                  | 3 (11, 0)                   | 1 (1, 0)                    | 1 (1, 0)    |
| <i>Diagnosis</i>               | (30) | 1669.00                   | 196 (341, 3)                | 76 ( 66, 0)                 | 43 ( 4, 0)                  | 118 (3, 2)                | 19 (338, 0)                 | 2 (39, 0)                   | 0 (1, 0)                    | 0 (1, 0)    |
| $\emptyset(\emptyset, \Sigma)$ |      | 190 (129, 11)             | 130 ( 48, 6)                | 315 ( 6, 45)                | 217 (2, 31)                 | 93 (105, 5)               | 72 (18, 10)                 | 168 (3, 18)                 | 101 (1, 21)                 |             |

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- *asprin<sub>w+s</sub>*
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- *s* — sign heuristic
- *1* — level-based heuristic
- *f* — factor-based heuristic
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- *1* — level-based heuristic
- *f* — factor-based heuristic

# *asprin* with different heuristic settings

| Benchmark \ System             |      | <i>asprin<sub>w</sub></i> | <i>asprin<sub>w+s</sub></i> | <i>asprin<sub>w+1</sub></i> | <i>asprin<sub>w+f</sub></i> | <i>asprin<sub>s</sub></i> | <i>asprin<sub>s+s</sub></i> | <i>asprin<sub>s+1</sub></i> | <i>asprin<sub>s+f</sub></i> |             |
|--------------------------------|------|---------------------------|-----------------------------|-----------------------------|-----------------------------|---------------------------|-----------------------------|-----------------------------|-----------------------------|-------------|
| <i>Ricochet</i>                | (30) | 20.00                     | 432 ( 8, 4)                 | 407 ( 7, 4)                 | 68 ( 1, 0)                  | 71 (1, 0)                 | 365 ( 8, 3)                 | 461 ( 7, 10)                | 69 (1, 0)                   | 71 (1, 0)   |
| <i>Timetabling</i>             | (12) | 23687.75                  | 345 (285, 3)                | 255 (202, 2)                | 900 ( 4, 12)                | 6 (1, 0)                  | 217 (144, 2)                | 21 (18, 0)                  | 900 (2, 12)                 | 5 (1, 0)    |
| <i>Puzzle</i>                  | (7)  | 580.57                    | 82 ( 2, 0)                  | 112 ( 2, 0)                 | 136 ( 2, 0)                 | 416 (2, 1)                | 31 ( 1, 0)                  | 32 ( 1, 0)                  | 21 (1, 0)                   | 51 (1, 0)   |
| <i>Crossing</i>                | (24) | 211.92                    | 104 ( 42, 1)                | 98 ( 35, 0)                 | 805 (19, 20)                | 387 (6, 6)                | 0 ( 6, 0)                   | 1 ( 6, 0)                   | 7 (9, 0)                    | 3 (1, 0)    |
| <i>Valves</i>                  | (30) | 56.63                     | 69 ( 7, 0)                  | 65 ( 6, 0)                  | 460 ( 8, 11)                | 715 (0, 22)               | 38 ( 4, 0)                  | 39 ( 4, 0)                  | 339 (4, 6)                  | 673 (0, 21) |
| <i>Expansion</i>               | (30) | 7501.87                   | 216 (299, 0)                | 10 ( 15, 0)                 | 38 ( 7, 0)                  | 12 (3, 0)                 | 64 (295, 0)                 | 14 (54, 0)                  | 4 (4, 0)                    | 3 (1, 0)    |
| <i>Repair</i>                  | (30) | 6750.73                   | 76 ( 48, 0)                 | 15 ( 47, 0)                 | 71 ( 3, 2)                  | 8 (2, 0)                  | 8 ( 43, 0)                  | 3 (11, 0)                   | 1 (1, 0)                    | 1 (1, 0)    |
| <i>Diagnosis</i>               | (30) | 1669.00                   | 196 (341, 3)                | 76 ( 66, 0)                 | 43 ( 4, 0)                  | 118 (3, 2)                | 19 (338, 0)                 | 2 (39, 0)                   | 0 (1, 0)                    | 0 (1, 0)    |
| $\emptyset(\emptyset, \Sigma)$ |      | 190 (129, 11)             | 130 ( 48, 6)                | 315 ( 6, 45)                | 217 (2, 31)                 | 93 (105, 5)               | 72 (18, 10)                 | 168 (3, 18)                 | 101 (1, 21)                 |             |

- *asprin<sub>w</sub>*
- *asprin<sub>w+s</sub>*
- *asprin<sub>w+1</sub>*
- *asprin<sub>w+f</sub>*
- *w* — weight-based
- *s* — sign heuristic
- *1* — level-based heuristic
- *f* — factor-based heuristic
- *asprin<sub>s</sub>*
- *asprin<sub>s+s</sub>*
- *asprin<sub>s+1</sub>*
- *s* — subset-based
- *s* — sign heuristic
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- *f* — factor-based heuristic

# *asprin* with different heuristic settings

| Benchmark \ System             |      | <i>asprin<sub>w</sub></i> | <i>asprin<sub>w+s</sub></i> | <i>asprin<sub>w+1</sub></i> | <i>asprin<sub>w+f</sub></i> | <i>asprin<sub>s</sub></i> | <i>asprin<sub>s+s</sub></i> | <i>asprin<sub>s+1</sub></i> | <i>asprin<sub>s+f</sub></i> |             |
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| <i>Valves</i>                  | (30) | 56.63                     | 69 ( 7, 0)                  | 65 ( 6, 0)                  | 460 ( 8, 11)                | 715 (0, 22)               | 38 ( 4, 0)                  | 39 ( 4, 0)                  | 339 (4, 6)                  | 673 (0, 21) |
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- *s* — subset-based
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- 1 Introduction
- 2 Declarative Problem Solving
- 3 An Example
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  - Dedicated systems versus asprin
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# *asprin* versus *clingo* and *metasp*

(B,D,R&S; AAAI)

| Benchmark \ System  |      | <i>clingo</i> | <i>asprin<sub>w</sub></i> | <i>asprin<sub>w</sub> -f</i> | <i>metasp</i> | <i>asprin<sub>s</sub></i> | <i>asprin<sub>s</sub> -f</i> |
|---------------------|------|---------------|---------------------------|------------------------------|---------------|---------------------------|------------------------------|
| <i>Ricochet</i>     | (30) | 20.00         | 104.74 (0)                | 174.26 ( 0)                  | 113.45 ( 0)   | 811.32 ( 24)              | 175.71 (0)                   |
| <i>Timetabling</i>  | (12) | 23687.75      | 35.82 (0)                 | 490.39 ( 5)                  | 694.92 ( 8)   | 798.75 ( 10)              | 142.03 (0)                   |
| <i>Puzzle</i>       | (7)  | 580.57        | 77.00 (0)                 | 77.39 ( 0)                   | 96.70 ( 0)    | 34.79 ( 0)                | 17.06 (0)                    |
| <i>Crossing</i>     | (24) | 211.92        | 48.43 (0)                 | 105.64 ( 1)                  | 67.50 ( 0)    | 62.33 ( 0)                | 0.50 (0)                     |
| <i>Valves</i>       | (30) | 56.63         | 52.53 (0)                 | 72.85 ( 0)                   | 78.11 ( 0)    | 900.00 ( 30)              | 45.01 (0)                    |
| <i>Expansion</i>    | (30) | 7501.87       | 91.53 (0)                 | 373.56 ( 2)                  | 241.05 ( 7)   | 900.00 ( 30)              | 292.57 (0)                   |
| <i>Repair</i>       | (30) | 6750.73       | 71.78 (0)                 | 102.19 ( 0)                  | 43.94 ( 0)    | 900.00 ( 30)              | 6.88 (0)                     |
| <i>Diagnosis</i>    | (30) | 1669.00       | 84.96 (0)                 | 254.19 ( 3)                  | 101.33 ( 0)   | 181.71 ( 6)               | 41.55 (0)                    |
| $\emptyset(\Sigma)$ |      | 70.85 (0)     | 206.31 (11)               | 179.63 (15)                  | 573.61 (130)  | 90.16 (0)                 | 25.47 (0)                    |

- *clingo* (using branch-and-bound)
- *asprin<sub>w</sub>*
- *asprin<sub>w</sub> -f*
- w — weight-based
- -f — no phase saving
- *metasp* (using disjunction)
- *asprin<sub>s</sub>*
- *asprin<sub>s</sub> -f*
- s — subset-based
- -f — no phase saving

# *asprin* versus *clingo* and *metasp*

(B,D,R&S; AAAI)

| Benchmark \ System  |      | <i>clingo</i> | <i>asprin<sub>w</sub></i> | <i>asprin<sub>w</sub> -f</i> | <i>metasp</i> | <i>asprin<sub>s</sub></i> | <i>asprin<sub>s</sub> -f</i> |
|---------------------|------|---------------|---------------------------|------------------------------|---------------|---------------------------|------------------------------|
| <i>Ricochet</i>     | (30) | 20.00         | 104.74 (0)                | 174.26 ( 0)                  | 113.45 ( 0)   | 811.32 ( 24)              | 175.71 (0)                   |
| <i>Timetabling</i>  | (12) | 23687.75      | 35.82 (0)                 | 490.39 ( 5)                  | 694.92 ( 8)   | 798.75 ( 10)              | 142.03 (0)                   |
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| <i>Valves</i>       | (30) | 56.63         | 52.53 (0)                 | 72.85 ( 0)                   | 78.11 ( 0)    | 900.00 ( 30)              | 45.01 (0)                    |
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- *clingo* (using branch-and-bound)
- *asprin<sub>w</sub>*
- *asprin<sub>w</sub> -f*
- w — weight-based
- -f — no phase saving
- *metasp* (using disjunction)
- *asprin<sub>s</sub>*
- *asprin<sub>s</sub> -f*
- s — subset-based
- -f — no phase saving

# aso versus asprin

| $n$                 | $aso$     | $aso_r$   | $asprin_a$ | $asprin_{r+a}$ |
|---------------------|-----------|-----------|------------|----------------|
| 350                 | 9 ( 0 )   | 17 ( 0 )  | 4 ( 0 )    | 5 ( 0 )        |
| 360                 | 14 ( 0 )  | 22 ( 0 )  | 48 ( 0 )   | 50 ( 0 )       |
| 370                 | 15 ( 0 )  | 25 ( 0 )  | 38 ( 0 )   | 39 ( 0 )       |
| 380                 | 10 ( 0 )  | 23 ( 0 )  | 8 ( 0 )    | 9 ( 0 )        |
| 390                 | 59 ( 0 )  | 72 ( 0 )  | 50 ( 1 )   | 52 ( 1 )       |
| 400                 | 22 ( 0 )  | 33 ( 0 )  | 28 ( 0 )   | 30 ( 0 )       |
| 410                 | 87 ( 1 )  | 96 ( 1 )  | 124 ( 2 )  | 125 ( 2 )      |
| 420                 | 97 ( 1 )  | 108 ( 1 ) | 60 ( 0 )   | 62 ( 0 )       |
| 430                 | 68 ( 0 )  | 79 ( 0 )  | 144 ( 0 )  | 147 ( 0 )      |
| 440                 | 165 ( 3 ) | 175 ( 3 ) | 165 ( 2 )  | 167 ( 2 )      |
| 450                 | 45 ( 0 )  | 61 ( 0 )  | 52 ( 0 )   | 54 ( 0 )       |
| 460                 | 112 ( 1 ) | 125 ( 1 ) | 117 ( 2 )  | 120 ( 2 )      |
| 470                 | 201 ( 4 ) | 210 ( 4 ) | 161 ( 2 )  | 162 ( 2 )      |
| 480                 | 152 ( 2 ) | 165 ( 2 ) | 70 ( 1 )   | 72 ( 1 )       |
| 490                 | 206 ( 2 ) | 218 ( 2 ) | 265 ( 4 )  | 267 ( 4 )      |
| $\emptyset(\Sigma)$ | 84 (14)   | 95 (14)   | 89 (14)    | 91 (14)        |

- $aso$  — dedicated system
- $aso_r$  — dedicated system with ranks
- $asprin_a$
- $asprin_{r+a}$  — with ranks

# *satpref* versus *asprin*

| Benchmark \ System             | <i>satpref</i> | <i>satpref+s</i> | <i>satpref+H</i> | <i>asprin<sub>p</sub></i> | <i>asprin<sub>p+s</sub></i> | <i>asprin<sub>p+H</sub></i> |
|--------------------------------|----------------|------------------|------------------|---------------------------|-----------------------------|-----------------------------|
| <i>0.0</i>                     | 0 ( 29, 0)     | 0 ( 1, 0)        | 0 (1, 0)         | 1 ( 16, 0)                | 0 ( 2, 0)                   | 0 (1, 0)                    |
| <i>0.00621</i>                 | 0 ( 35, 0)     | 0 ( 1, 0)        | 90 (1, 6)        | 1 ( 17, 0)                | 1 ( 2, 0)                   | 1 (1, 0)                    |
| <i>0.01243</i>                 | 1 ( 75, 0)     | 1 ( 3, 0)        | 118 (1, 7)       | 6 ( 26, 0)                | 2 ( 3, 0)                   | 3 (1, 0)                    |
| <i>0.02486</i>                 | 8 ( 388, 0)    | 6 ( 10, 0)       | 635 (1, 38)      | 55 ( 74, 0)               | 9 ( 8, 0)                   | 64 (1, 4)                   |
| <i>0.04972</i>                 | 67 ( 1463, 2)  | 16 ( 36, 0)      | 900 (0,100)      | 318 (203, 16)             | 26 (17, 0)                  | 176 (1,14)                  |
| <i>1.0</i>                     | 850 (10315,88) | 243 (590,10)     | 177 (1, 12)      | 856 (323, 92)             | 174 (96, 0)                 | 280 (1,24)                  |
| $\emptyset(\emptyset, \Sigma)$ | 154 ( 2051,90) | 44 (107,10)      | 320 (1,163)      | 206 (110,108)             | 35 (21, 0)                  | 88 (1,42)                   |
| <i>MAXSAT</i>                  | 54 ( 8849, 0)  | 9 ( 7, 0)        | 62 (1, 0)        | 835 (957, 31)             | 109 (31, 3)                 | 171 (1, 6)                  |
| <i>PBO/pbo-mqc-nencdr</i>      | 5 ( 267, 0)    | 2 ( 2, 0)        | 664 (1, 88)      | 150 (207, 14)             | 9 ( 2, 0)                   | 244 (1,20)                  |
| <i>PBO/pbo-mqc-nlogencdr</i>   | 3 ( 228, 0)    | 1 ( 2, 0)        | 237 (1, 21)      | 110 (214, 3)              | 5 ( 2, 0)                   | 141 (1,15)                  |
| <i>PSEUDO/primes</i>           | 110 ( 396,18)  | 110 ( 1,18)      | 110 (1, 18)      | 215 (334, 27)             | 106 ( 5,17)                 | 110 (1,17)                  |
| <i>PSEUDO/routing</i>          | 346 ( 409, 4)  | 49 ( 1, 0)       | 50 (1, 0)        | 85 (475, 0)               | 4 ( 1, 0)                   | 86 (1, 1)                   |
| <i>Partial-MINONE</i>          | 14 ( 2, 0)     | 14 ( 2, 0)       | 7 (1, 0)         | 24 ( 2, 0)                | 24 ( 1, 0)                  | 25 (1, 0)                   |
| $\emptyset(\emptyset, \Sigma)$ | 88 ( 1692,22)  | 31 ( 2,18)       | 188 (1,127)      | 236 (365, 75)             | 43 ( 7,20)                  | 129 (1,59)                  |

- *satpref*
- *satpref+s*
- *satpref+H*
- s — sign heuristic
- H — complex heuristic
- *asprin<sub>p</sub>*
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- *asprin* stands for “ASP for Preference handling”
- *asprin* is a general, flexible, and extendable framework for preference handling in ASP
- *asprin* caters to
  - off-the-shelf users using the preference relations in *asprin*'s library
  - preference engineers customizing their own preference relations
- *asprin* can be boosted by *clingo*'s heuristic framework
- <https://github.com/potassco/asprin>

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